NASA Sun-Earth Connections Theory Program Contract NAS5-99188

The Structure and Dynamics of the Solar Corona and Inner Heliosphere

FOURTH QUARTER SECOND YEAR PROGRESS REPORT Covering the period May 16, 2001 to August 15, 2001

Submitted by:

Zoran Mikić
Principal Investigator
Science Applications International Corporation
10260 Campus Point Drive
San Diego, CA 92121

August 15, 2001

FOURTH QUARTER SECOND YEAR PROGRESS REPORT

This report covers technical progress during the fourth quarter of the second year of NASA Sun-Earth Connections Theory Program (SECTP) contract "The Structure and Dynamics of the Solar Corona and Inner Heliosphere," NAS5-99188, between NASA and Science Applications International Corporation, and covers the period May 16, 2001 to August 15, 2001. Under this contract SAIC and the University of California, Irvine (UCI) have conducted research into theoretical modeling of active regions, the solar corona, and the inner heliosphere, using the MHD model.

Press Release at the Spring AGU Meeting, Boston, MA, May 30, 2001

Zoran Mikić was invited by the AAS/SPD press officer, Dr. Criag DeForest, to give a presentation at a press conference about the total solar eclipse that was expected in Africa on June 21, 2001. An accompanying press release is contained in Appendix A.

Presentations at the Spring AGU Meeting, Boston, MA, May 29-June 2, 2001

Our progress during this reporting period is summarized by the following papers that were presented by SAIC staff members at the Spring AGU Meeting, Boston, MA, May 29–June 2, 2001.

Predicting the Structure of the Solar Corona During the 21 June 2001 Total Solar Eclipse

Z. Mikić, J. A. Linker, R. Lionello, and P. Riley (SAIC, San Diego)

We describe the application of a three-dimensional magnetohydrodynamic (MHD) model to the prediction of the structure of the corona during the total solar eclipse that is expected to occur on 21 June 2001. The calculation uses the observed photospheric radial magnetic field as a boundary condition. This model makes it possible to determine the large-scale structure of the magnetic field in the corona, as well as the distribution of the solar wind velocity, plasma density, and temperature. We will use magnetic fields observed on the solar disk prior to eclipse day to predict what the corona will look like during the eclipse. The estimated coronal density will be used to predict the plane-of-sky polarization brightness prior to the eclipse.

A copy of this presentation appears in Appendix B.

Are There Two Classes of Coronal Mass Ejections? A Theoretical Perspective*

J. A Linker, Z. Mikić, R. Lionello, and P. Riley (SAIC, San Diego)

Coronal mass ejections (CMEs) are generally accepted as the cause of nonrecurrent generally generally accepted as the cause of nonrecurrent generally gene

the examination of the acceleration profiles of CMEs has led to the possible classification of CMEs as either constant speed CMEs or constant acceleration (St. Cyr et al., JGR 104, 12493, 1999; Sheeley et al., JGR 104, 24739, 1999). In this talk, we will examine reasons why one might expect CMEs to show two classes of acceleration profiles, and if they do, what the implications are for models of CME initiation. Examples from MHD simulations of CMEs for different initiation mechanisms will be used to illustrate essential points.

*Research supported by NASA and Boston University's Integrated Space Weather Modeling project (funded by NSF).

A copy of this presentation appears in Appendix C.

Using Global MHD Simulations to Interpret In Situ Observations of CMEs

P. Riley, J. A. Linker, R. Lionello, Z. Mikić (SAIC, San Diego)

D. Odstrcil, V. J. Pizzo (SEC, Boulder)

T. H. Zurbuchen (U. Michigan)

D. Lario (JHU/APL)

In this study, we combine two MHD models to simulate the initiation, propagation, and dynamic evolution of flux-rope-like CMEs through the corona and out to 1 AU. The coronal model encompasses the region of the solar corona from $1R_s$ to $20R_s$, while the heliospheric model encompasses $20R_s$ to 1 AU. The CME initiated in the corona propagates smoothly across the outer boundary of the coronal solution and through the inner boundary of the heliospheric solution. The model solutions show a rich complexity, which, given the relative simplicity and idealization of the input conditions, bear a strong resemblance to many observed events, and we use the simulation results to infer the global structure of some of these observations. In particular, we highlight an event that was observed by both Ulysses and ACE in February/March, 1999. At this time, Ulysses was located at ~ 5 AU and 22°S heliographic latitude; thus the two spacecraft were separated significantly both in heliocentric distance and latitude. We also use these simulations to separate dynamical effects from force-free models of flux ropes in the solar wind.

A copy of this presentation appears in Appendix D.

Modeling of Transequatorial Loops with MH4D

R. Lionello and D. Schnack (SAIC, San Diego)

MH4D (Magnetohydrodynamics on a TETRAhedral Domain) is a new algorithm to perform magnetohydrodynamic (MHD) simulations of the active regions of the Sun, including the large scale coronal structure that surround them. MH4D is a massively-parallel, device-independent numerical code for the advancement of the resistive and viscous MHD equations on an unstructured grid of tetrahedra. The use of an unstructured grid allows us to increase the resolution in the regions of physical interest. A variational formulation of the differential operators ensures accuracy and the preservation of the analytical properties of the operators

 $(\nabla \cdot \mathbf{B} = 0$, self-adjointness of the resistive and viscous operators). The combined semi-implicit treatment of the waves and implicit formulation of the diffusive operators can accommodate the wide range of time scales present in the solar corona. The capability of mesh refinement and coarsening is also included. A preliminary result is presented: a simulation of transequatorial loops that include fine details of two interconnected active regions.

A copy of this presentation appears in Appendix E.

APPENDIX A

Press Release at the Spring AGU Meeting Boston, MA, May 30, 2001 Presented by Zoran Mikić

PREDICTING THE STRUCTURE OF THE SOLAR CORONA DURING THE 21 JUNE 2001 TOTAL SOLAR ECLIPSE

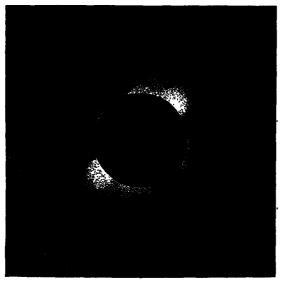
Total solar eclipses offer an excellent opportunity to observe the solar corona. During a total solar eclipse the moon blocks the bright light from the solar disk, allowing the faint light scattered by the solar corona, which is more than a million times fainter than the photosphere, to become visible. During totality the structures that characterize the white-light corona become apparent, including prominences, helmet streamers, polar plumes, and coronal holes. Observers who witness a total solar eclipse invariably report that it is a beautiful sight to behold.

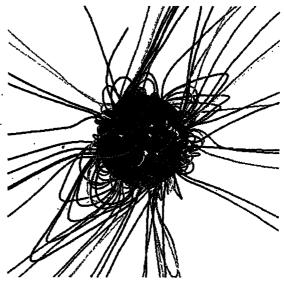
On 21 June, 2001 a total eclipse of the Sun will be visible in the southern hemisphere, beginning in the South Atlantic, crossing southern Africa and Madagascar, and terminating in the Indian Ocean. Drs. Zoran Mikić, Jon Linker, Pete Riley, and Roberto Lionello, of Science Applications International Corporation (SAIC) in San Diego, California, have developed a theoretical model to predict what the solar corona will look like during forthcoming total solar eclipses. Their model has been used to predict the shape of the corona during the eclipse that is expected to occur on 21 June.

The model is based on the three-dimensional magnetohydrodynamic (MHD) equations that describe the interaction of the solar wind with coronal magnetic fields. The group's results, which have been financially supported by the National Aeronautics and Space Administration (NASA) and the National Science Foundation (NSF), are being presented by Dr. Mikić at the American Geophysical Union meeting in Boston.

The calculation relies on Earth-based measurements of the magnetic field in the solar photosphere to infer the structure of the solar corona. The measurements are taken at the National Solar Observatory at Kitt Peak. "It is remarkable that measurements of the magnetic field in the photosphere can tell us so much about the corona," says Dr. Mikić. "The simulations already have a strong resemblance to coronal images. In the future, the agreement will only improve as we refine the physics in our model and as we utilize ever-faster computers. We will be able to study even finer details in the corona." The researchers use supercomputers at the San Diego Supercomputer Center (part of NSF's National Partnership for Advanced Computing Infrastructure) and the Department of Energy's National Energy Research Supercomputer Center to solve the equations. The output from the model is used to predict the brightness of the corona.

So far, this model has been applied to five eclipses (see http://haven.saic.com). This kind of modeling helps us to understand the structure of the solar corona, especially the location of helmet streamers and coronal holes, and the nature of the fast and slow solar wind, and provides a rudimentary test of predictive capability. Eclipses offer an opportunity to test such models, and to understand the influence of the Sun on the Earth.





Predicted polarization brightness (pB) for the 21 June, 2001 eclipse, together with traces of the magnetic field lines, at 13:10 UT (corresponding to totality in Lusaka, Zambia). The pB signal is produced by white light scattered off electrons in the coronal plasma. This is the view of the Sun that would be seen by an observer on Earth with a camera aligned so that vertical is toward the Earth's north pole.

APPENDIX B

"Predicting the Structure of the Solar Corona During the 21 June 2001 Total Solar Eclipse"

Z. Mikić, J. A. Linker, R. Lionello, and P. Riley

Presented at the Spring AGU Meeting

Boston, MA, May 29–June 2, 2001

PREDICTING THE STRUCTURE OF THE STAR CORONA DURING THE STAR CORONA DURING THE STAR CORONA DURING TOTAL SOLAR ECLIPSE*

ZORAN MIKIĆ

JON A. LINKER

PETE RILEY

ROBERTO LIONELLO

SCIENCE APPLICATIONS INTL. CORP.
SAN DIEGO

Presented at the Meeting of the American Geophysical Union, Boston, May 29–June 2, 2001

*Supported by NASA and NSF

INTRODUCTION

- The solar magnetic field plays a key role in determining coronal
- The principal input to MHD models is the observed solar magnetic field
- 3D MHD models can be used to compare with eclipse and coronagraph images, SOHO images (LASCO, EIT), Ulysses and WIND spacecraft data, and interplanetary scintillation (IPS) measurements
- MHD computations can tell us about the structure of the corona
- Eclipses can help us to verify the accuracy of the models
- 21 June, 2001 total solar eclipse: visible in the southern hemisphere, (South Atlantic, southern Africa, Madagascar, and Indian Ocean)
- Totality in Lusaka, Zambia is at 13:10UT

Manage Equations

$$\nabla \times \vec{B} = \frac{4\pi}{c} \mathbf{J}$$

$$\nabla \times \vec{B} = -\frac{1}{c} \frac{\partial \mathbf{B}}{\partial t}$$

$$\mathbf{E} + \frac{1}{c} \mathbf{v} \times \mathbf{B} = \eta \mathbf{J}$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\rho \left(\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right) = \frac{1}{c} \mathbf{J} \times \mathbf{B} - \nabla \rho - \nabla \rho_w + \rho \mathbf{g} + \nabla \cdot (\nu \rho \nabla \mathbf{v})$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = (\gamma - 1)(-\rho \nabla \cdot \mathbf{v} + S)$$

THE POLYTROPIC MODEL

- Neglect thermal conduction, coronal heating, radiation loss, and Alfvén waves (set $p_w = 0$ and S = 0)
- Simulate these effects (crudely) by setting $\gamma = 1.05$ (Parker 1963)
- A possible extension is to have $\gamma = \gamma(r)$, with γ increasing far from the Sun
- We have used this model extensively in 3D computations of the structure and dynamics (e.g., CMEs) of the solar corona
- The corona is modeled reasonably well, but the properties of the interplanetary solar wind are not accurate (speed, density, temperature)
- An improved model (with more accurate energy transport) is being developed

MHD EQUATIONS (POLYTROPIC MODEL)

$$\nabla \times \mathbf{B} = \frac{4\pi}{c} \mathbf{J}$$

$$\nabla \times \mathbf{E} = -\frac{1}{c} \frac{\partial \mathbf{B}}{\partial t}$$

$$\mathbf{E} + \frac{1}{c} \mathbf{v} \times \mathbf{B} = \eta \mathbf{J}$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\rho \left(\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right) = \frac{1}{c} \mathbf{J} \times \mathbf{B} - \nabla \rho + \rho \mathbf{g} + \nabla \cdot (\nu \rho \nabla \mathbf{v})$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = -(\gamma - 1) \rho \nabla \cdot \mathbf{v}$$

$$\gamma = 1.05$$

1 1

FINDING MHD SOLUTIONS

- Use line-of-sight magnetograms to deduce B_r from B_{los} at $r = R_o$ (e.g., Kitt Peak Solar Observatory and Wilcox Solar Observatory synoptic maps)
- Calculate a potential field matching B_r at $r = R_0$
- Specify T and ρ on the solar surface $r = R_0$ (e.g., uniform T_0 and ρ_0)
- Set up p, ρ , and v from a spherically symmetric solar wind (1D Parker solution)
- Integrate 3D MHD equations in time until steady state is reached
- This gives the structure of the coronal magnetic field **B** (as well as p, ρ , \mathbf{v} , T)
- Compare with observations

POLARIZATION BRIGHTNESS

 Light scattered off the coronal electrons is observed in coronagraphs

$$pB(\mathbf{x}) = K \int_{\log \mathbf{x}} n_e(\mathbf{x} - \mathbf{x}') C(r') dl'$$

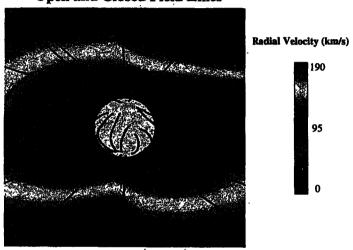
- *C*(*r*) is a scattering function (*e.g.*, Billings 1966)
- To produce a plane-of-sky image, we apply a (radial) filter to *pB* ("vignetting function") and we simulate the effect of an occulting disk

"CANONICAL" HELMET STREAMER

- Idealized helmet streamer configuration
- Start with 2D (axisymmetric) dipole field (Pneuman & Kopp 1971)
- Closed-field region with a static (v = 0) dense plasma, surrounded by an openfield region with solar wind streaming along the field lines
- A current sheet surrounds the helmet, and an equatorial current-sheet separates fields of opposite polarity

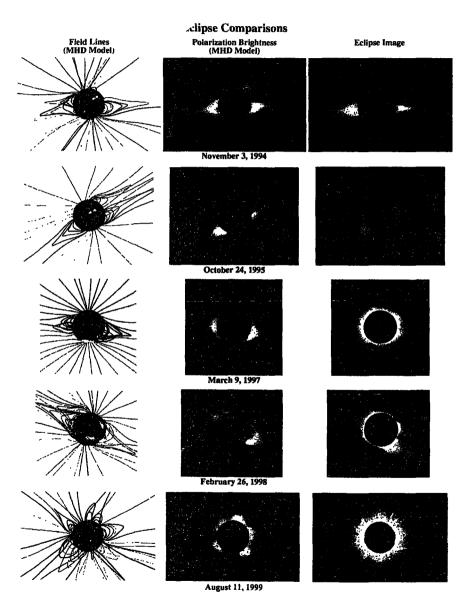
Visole Sun MonthAug. 10 – Sep. 8, 1996

Radial Velocity
Open and Closed Field Lines



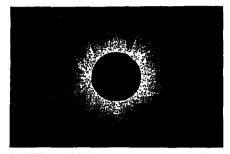
COMPARISON WITH ECLIPSE AND CORONAGRAPH OBSERVATIONS

- November 3, 1994 eclipse (Chile)
 Compare with eclipse image (HAO) and Mauna Loa coronagraph data
- October 24, 1995 eclipse (Vietnam):
 We predicted the coronal structure on Oct. 5, 1995
 Compare with eclipse image (S. Koutchmy)
- March 9, 1997 eclipse (Russia, China, & Mongolia):
 We predicted the coronal structure on Mar. 3, 1997
 Compare with eclipse image (E. Hiei)
- February 26, 1998 eclipse (Carribean):
 We predicted the coronal structure on
 Feb. 13, 1998
 Compare with eclipse image (HAO)

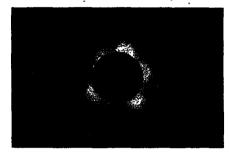


 August 11, 1999 eclipse (Central Europe, Turkey, Iran):
 We predicted the coronal structure on July 28, 1999
 Compare with eclipse image (Espenak)

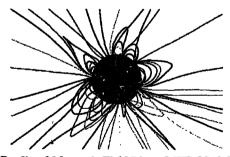
Comparison of a 3D MHD Coronal Prediction with an Image of the 11 August 1999 Total Solar Eclipse



Fred Espenak's Composite Image (Turkey)



Predicted Polarization Brightness (MHD Model)

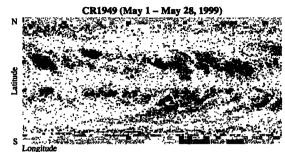


Predicted Magnetic Field Lines (MHD Model)

Figure 1. Comparison between a composite eclipse image created from photographs taken by Fred Espenak in Lake Hazar, Turkey (top) with the predicted polarization brightness of the simulated solar corona from our 3D MHD model (middle). The projected magnetic field lines from the model are also shown (bottom). Terrestrial (geocentric) north is vertically upward. The eclipse image is copyrighted 1999 by Fred Espenak.

Evolution of the Photospheric Magnetic Field Leading up to the August 11, 1999 Total Solar Eclipse

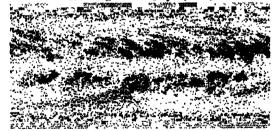
(Courtesy of Kitt Peak Solar Observatory)



CR1950 (May 28 - June 24, 1999)



CR1951 (June 24 - July 21, 1999)

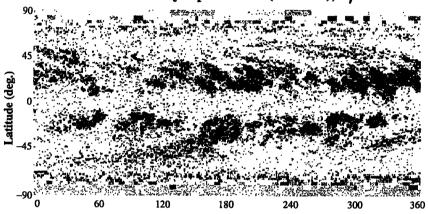


CD1051+1052 (Inly 13 - Angust 5 1000)

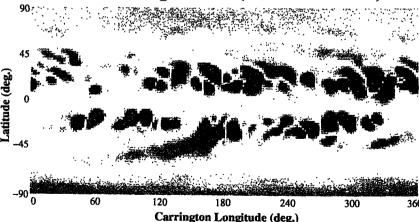


August 11, 1999 Total Solar Eclipse





Smoothed Magnetic Field (used in MHD model)



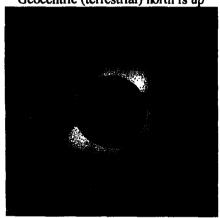
JUNE 21, 2001 SOLAR ECLIPSE PREDICTION

- Started a high-resolution simulation on May 19, 2001 using magnetic field data from a Kitt Peak Solar Observatory synoptic map of CR1975 (April 9–May 6, 2001).
- Low-resolution case: $61 \times 71 \times 64$ (r,θ,ϕ) mesh points $(\sim 7 \text{ CPU hrs on the Cray-T90})$
- High-resolution case: $111 \times 101 \times 128$ (r, θ, ϕ) mesh points $(\sim 90 \text{ CPU hrs on the Cray-T90})$
- This calculation will be updated in the next few weeks with more recent magnetic field data
- The code runs on PCs and Cray computers. It is also being developed to run on massively parallel machines using MPI (e.g., Cray T3E, Beowulf, IBM SP3)
- See:

http://haven.saic.com/corona/modeling.html

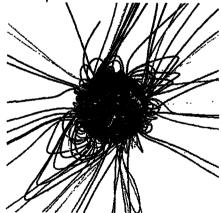
Prediction of the Structure of the Solar Corona for the 21 June 2001 Eclipse

Predicted Polarization Brightness Geocentric (terrestrial) north is up



Magnetic Field Lines

B, contoured on the surface



Predicted on May 19, 2001 using magnetic field data from Kitt Peak Solar Observatory for Carrington rotation 1975 (April 9 - May 6, 2001).

http://haven.saic.com

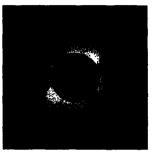
y 29 2001 June 21 2001 Scient Echane



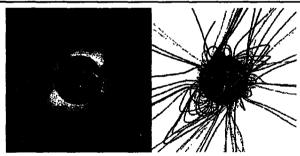
Predicting the Structure of the Solar Corona During the 21 June, 2001 Total Solar Eclipse

On Thursday, 21 June, 2001, a total eclapse of the Sun will be visible from within a narrow corridor crossing the Southern Hemisphere, beginning in the South Atlantic, crossing southern Africa and Madagascar, and terminating in the Indian Ocean. A partial eclipse can be seen droughout eastern South America and mind south Africa. To see a declared description of the eclipse path, please visit <u>Fired Expended, 2001 Total Eclipse, web site</u>

On 19 May, 2001, we started an MHD computation of the solar corona, in preparation for our prediction of what the solar corona will look like during this eclipse. We used photospheric magnetic field data from Carrington rotation 1973 (corresponding to the dates April 9 - May 6, 2001) Iron the National Solar Observatory at Kin Peak. We will update this prediction in the next few weeks using more recent photospheric magnetic field data. After the eclipse we will publish comparisons between our prediction and images taken on the day of the eclipse.



The figure on the left shows the predicted polarization brightness (pB) in the solar corona for the eclipse expected on 21 June, 2001 at 13:10 UT (corresponding to totality in Lusaka, Zambia). The state of the solar corona was computed using a 3D magnetolythodynamic (MHD) minulation. The pB signal is produced by white leght scattered off electrons in the coronal pleana. The unage has been radially deterned to account for the fall-off of coronal brightness with distance from the Sun. Vertical (top) is terrestrial (geocentric) north. This is the view of the Sun that would be seen by an observer on Earth with a causer aligned so that vertical is toward the Earth's north pole. To view thys image in a coordinate system aligned with solar north, <u>click here.</u> Click the image to see it in more detail



Predicted polarization brightness (top left) together with traces of the magnetic field lines in the solar corona (top right) for the eclipse expected on 21 June, 2001 at 13 10 UT (with terrestinal north up). The Sun's surface shows color contours of the radial component of the measured photospheric magnetic field from <u>Kitt Peak National Solar Observators</u>, showing the location of active regions (strong magnetic fields). Click the images for higher resolution pretures. To view these images an a coordinate system adapted with solar north, elick here.

lile ///powerbook HD/Desktop*s20Folder#Etipse*s2020016Haven*s20Web*s20Pege/

June*+2021*+2C*+202001*+205dle*+205dlepee

uesday May 29 2001

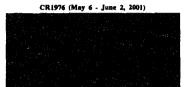
Page 2

CR1975 (April 9 - May 6, 2001)

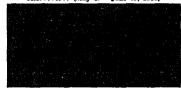


The photospheric magnetic field maps we use for our calculations are built up from duly observations of the Sun during a solar rotation. These maps give a good approximation of the Sun's magnetic flux if the large-scale flux is not changing much throughout a rotation. Previously, we have computed covoral models for an eclapse during the declining phase of the last solar cycle (November 3, 1928), for two eclipses during solar minimum (Dichotar 24, 1929, and March 9, 1929), one eclipse during the minimum (Dichotar 24, 1929, and March 9, 1929), one competed uring the the early rising phase of solar cycle 23 (February 26, 1928), and one eclipse approaching solar maximum (August 11, 1929). The June 21, 2001 eclipse, which is occurring at the peak of solar maximum, presents a challenge. The photospheric magnetic field data a less reliable approximation to the true state of the photospheric magnetic field data a less reliable approximation to the true state of the photospheric magnetic field. The complexity of coronal structures requires high resolution truns (requiring approximately 1,500,000 grid points in our calculation).

These figures show the photosphene magnetic field maps for three Carrington rotations, CR1975, CR1976, and CR1976+1977, as measured by the National Solar Observatory at Kitt Peak. The maps show the measured photosphene magnetic field as a function of lattude (vertical axis) and Carrington longitude (horizontal axis) Red shows outward directed magnetic flux, and blue shows inward directed flux Click the images for higher resolution pictures. These maps are considerably more complex than mapa during solar minimum.



CR1976+1977 (May 19 - June 15, 2001)



Movies:

We have made a movie of the polarization brightness from our MHD simulation of the solar corona during Carrington rotation 1975 (April 9 - May 6, 2001). This illustrates vicinity have rapidly the solar corona changes as a result of solar rotation during the maximum phase of the solar cycle. You can get an MPEG version (359 kbytes).

If your movie player can continuously loop a movie while playing it, set this option to "on" for the best effect. For example on a Silicon Graphics machine, you would use the execute line movieplayer (10 or 1975 mpg

Other web resources for the eclipse:

- Fred Expense's 2001 Total Solar Eclipse web site (A great resource for the eclipse, including lots of information and links to other sites)
 Eclipse information from NASA's Goddard Space Flight Cepter
 Sky and Telescope Magazine
 IAU Working Group on Eclipses
 IAU Working Group on Eclipses



Return to the Coronal Modeling Page

APPENDIX C

"Are There Two Classes of Coronal Mass Ejections? A Theoretical Perspective"

J. A Linker, Z. Mikić, R. Lionello, and P. Riley

Presented at the Spring AGU Meeting

Boston, MA, May 29-June 2, 2001

ARE THERE TWO CLASS OF CORONAL MASS EJECTIONS?

A TEEORETICAL PIESPECTIVE*

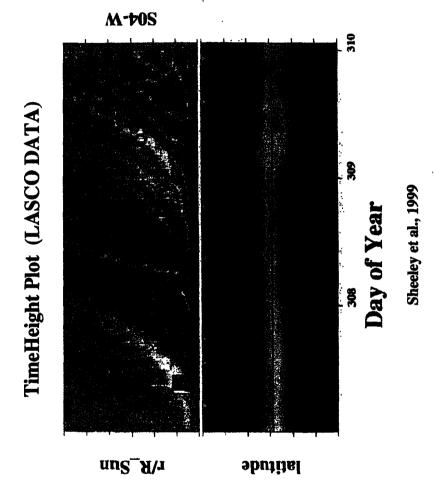
JON A. LINKER
ZORAN MIKIC
ROBERTO LIONELLO
PETE RILEY

Science Applications International Corporation

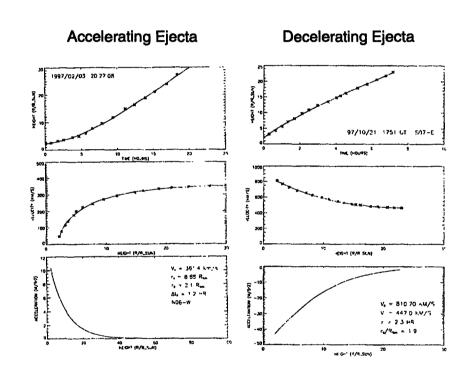
*Research Supported by NASA and NSF (through Boston University's Integrated Space Weather Modeling Project). Computations performed at NPACI/SDSC.

INTRODUCTION

- Despite many years of study, the origin evolution and of coronal mass ejections (CMEs) is poorly understood.
- What are the underlying physical differences between "fast" and "slow" CMES? ⇒ Important for Space Weather
- Recently, it has been demonstrated that many CMEs observed with the LASCO coronagraph fall roughly into two classes (Sheeley et al. 1999):
 - (1) CMEs that accelerate up to an asymptotic speed;
 - (2) CMEs that travel at constant speed or decelerate



From Sheeley et al., 1999



MY "ASSIGNMENT:"

"The modelers should address the question of whether there is any theoretical reason why an accelerating CME requires a different expulsion mechanism or environment than a CME that starts out fast and then decelerates.

They should ask themselves whether they can produce the different speed profiles just by varying the source region....

Of course they should also suggest other reasons they can think of that might result in the different speed profiles. "

QUESTIONS

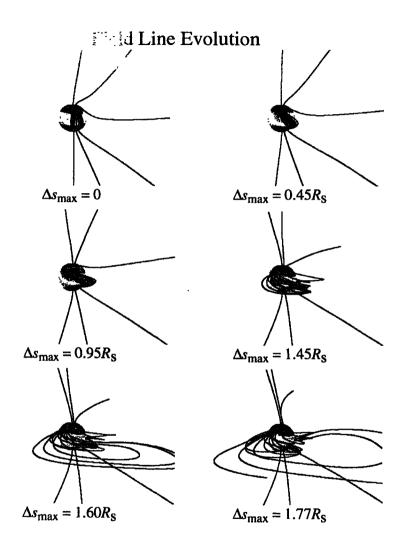
- Does the division of CMEs into "accelerating" and "constant speed" imply more than one mechanism for CMEs initiation? Does it imply only one mechanism?
- Can we use this classification to help us to understand CME initiation or constrain the possible mechanisms?

MECHANISMS FOR SOLAR ACTIVITY

- CMEs, flares, and prominence eruptions require significant amounts of energy (~10³² ergs)
- Most theories assume that energy is released from the coronal magnetic field (see next talk for an opposing view)
- There are many observations of nonpotential magnetic field structures in the corona harboring significant amounts of magnetic energy
- What causes this energy to be released? Many candidate mechanisms
- What sort of time-height profiles of ejecta are implied by different mechanisms? Today we consider two:
 - (1) Shearing of the photospheric magnetic field
 - (2) Magnetic flux cancellation

ERUPTION BY PHOTOSPHERIC SHEARING FLOWS

- Previously, we showed that photospheric shear leads to the eruption of magnetic field arcades and helmet streamers if the photospheric shear exceeds a threshold (Mikic &Linker 1994, Linker &Mikic1995)
- Start from a helmet streamer configuration
- Introduce flows (typically 0.5-5 km/s) at the photosphere that twist or shear the magnetic field and energize the configuration.
- When the magnetic shear crosses a threshold, eruption occurs. Eruption threshold does not depend on how fast the shear is introduced.
- Eruption is related to Magnetic
 Nonequilibrium the appearance of a
 discontinuity in force-free equilibrium
 configurations

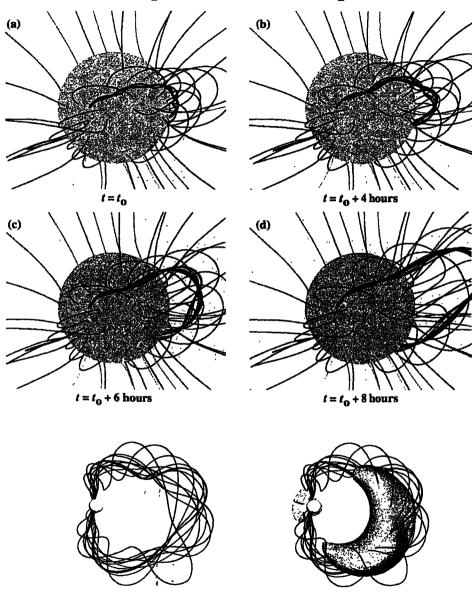


Eruption of a 3D Helmet Streamer triggered Shearing Flows

ERUPTION BY FLUX CANCELLATION

- We have found that reduction of magnetic flux near the neutral line of a sheared or twisted magnetic configuration (i.e., flux cancellation) can lead to the formation of stable flux rope configurations (Amari et al , 1999, 2000; Linker et al, 2001)
- The flux ropes are capable of supporting prominence material in the corona
- When the flux cancellation crosses a threshold, the entire configuration erupts. In the case of a helmet streamer configuration, a CME is ejected into the simulated solar wind.
- The eruption is more energetic than eruptions triggered by photospheric shearing flows.

Eruption of a 3D Flux Rope



CONSIDER 5 MODEL PROBLEMS:

- Vary mechanism: Shearing and Flux cancellation
- Vary initial corona: Base temperature 1.4X10⁶ K or 1.8X10⁶ K (solar wind speeds of 250 km/s or 350 km/s at 20R_s
- Performed one flux cancellation simulation with broader shear distribution

MHD EQUATIONS

$$\nabla \times \mathbf{B} = \frac{4\pi}{c} \mathbf{J}$$

$$\nabla \times \mathbf{E} = -\frac{1}{c} \frac{\partial \mathbf{B}}{\partial t}$$

$$\mathbf{E} + \frac{1}{c} \mathbf{v} \times \mathbf{B} = \eta \mathbf{J}$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\rho \left(\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right) = \frac{1}{c} \mathbf{J} \times \mathbf{B} - \nabla \rho + \rho \mathbf{g} + \nabla \cdot (\nu \rho \nabla \mathbf{v})$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = (\gamma - 1)(-\rho \nabla \cdot \mathbf{v} + S)$$

Helmet Streamer Configuration for CME Studies

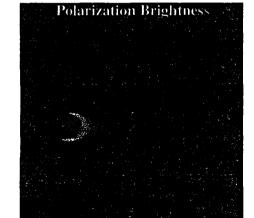
Flux $\Psi(r,z)$



Initial Potential Field

Relaxed Helmet Streamer

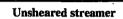
Current Density $J_{\phi}(r,z)$

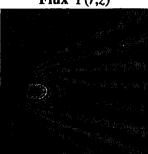


Relaxed Helmet Streamer

Eruption of a Helmet Streamer By Emerging Flux

Flux $\Psi(r,z)$





Sheared streamer $t = t_0$



4.5% emerged flux $t = t_0 + 6$ hours



7.5% emerged flux $t = t_0 + 10$ hours



10.5% emerged flux $t = t_0 + 14$ hours



12% emerged flux $t = t_0 + 16$ hours



13.5% emerged flux $t = t_0 + 18$ hours



15% emerged flux $t = t_0 + 20$ hours



15% emerged flux $t = t_0 + 2.5 \text{ days}$

Eruption of a Helmet Streamer By Emerging Flux

Polarization Brightness



Unsheared streamer



Sheared streamer $t = t_0$



4.5% emerged flux $t = t_0 + 6 \text{ hours}$



7.5% emerged flux $t = t_0 + 10$ hours



10.5% emerged flux $t = t_0 + 14$ hours



12% emerged flux $t = t_0 + 16 \text{ hours}$



13.5% emerged flux $t = t_0 + 18$ hours

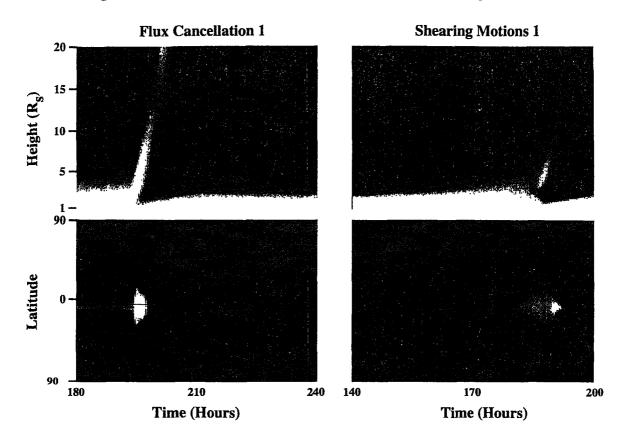


15% emerged flux $t = t_0 + 20$ hours

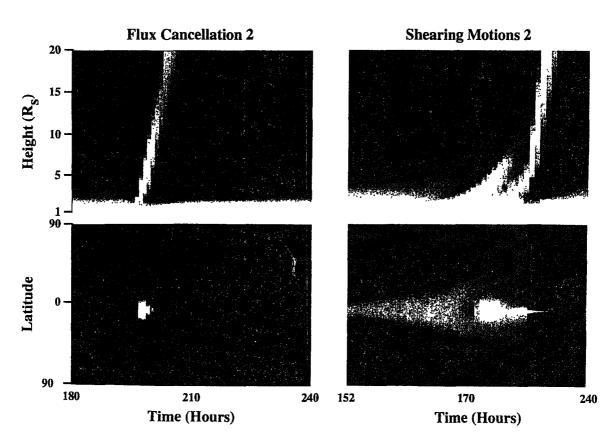


15% emerged flux $t = t_0 + 2.5 \text{ days}$

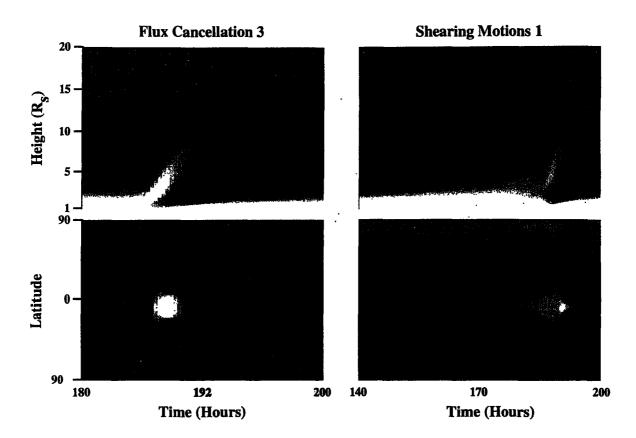
TimeHeight Profiles: Flux Cancellation and Shearing Simulations

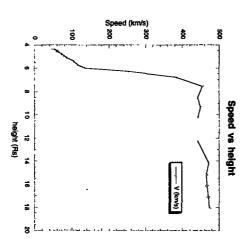


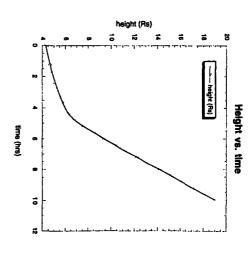
TimeHeight Profiles: Slower Solar Wind



TimeHeight Profiles:



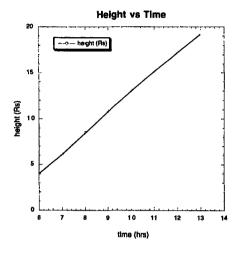


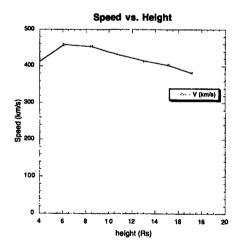


 $\mathbb{R}(\mathcal{C}^{\infty})^{\mathrm{Sp}}_{\mathcal{C}}$

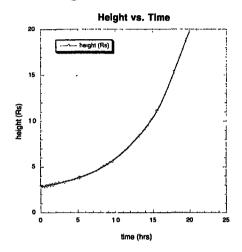
Flux Cancellation, Medium Wind Background

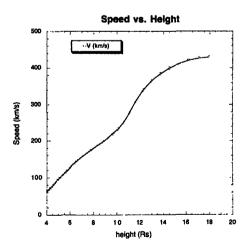
Flux Cancellation, Slow Wind Background



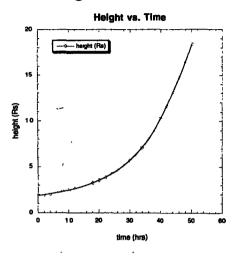


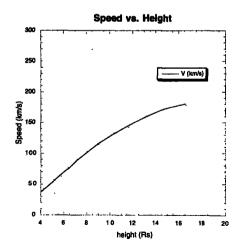
Shearing Flows, Medium Wind

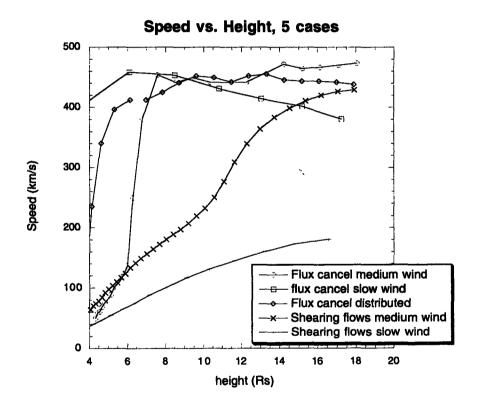




Shearing Flows, Slow Wind







SUMMARY

- We examined the results from simulated CMEs initiated by magnetic flux cancellation and by photospheric shearing flows.
- The flux cancellation CMEs yielded either accelerating or constant speed ejecta depending on the properties of the ambient solar wind.
- The CMEs initiated by photospheric shearing flows yielded accelerating ejecta. Shearing flow simulations with other initial configurations might also yield constant speed ejecta.

WHAT HAVE WE LEARNED?

Questions I raised at the beginning of the talk:

- Does the rough division of CMEs into "accelerating" and "constant speed" imply more than one mechanism for CMEs initiation? No.
- Does this division imply that CMEs are initiated by only one mechanism? No.
- Can this classification by itself help us to understand CME initiation or constrain the possible mechanisms?
- Our results suggest that the approximate division of CMEs into "accelerating" or "constant speed" is a natural consequence of having a range of energy inputs and diverse solar wind conditions for different CME ejecta.

APPENDIX D

"Using Global MHD Simulations to Interpret In Situ Observations of CMEs"
P. Riley, J. A. Linker, R. Lionello, Z. Mikić, D. Odstrcil, V. J. Pizzo,
T. H. Zurbuchen, and D. Lario
Presented at the Spring AGU Meeting
Boston, MA, May 29-June 2, 2001

Using Global MHD Simulations to Interpret in situ Observations of CMEs

Pete Riley, J. A. Linker, Z. Mikic

SAIC, San Diego, California

D. Odstrcil, V. J. Pizzo

NOAA/SEC, Boulder, Colorado

T. H. Zurbuchen

University of Michigan

D. Lario

JHU/APL

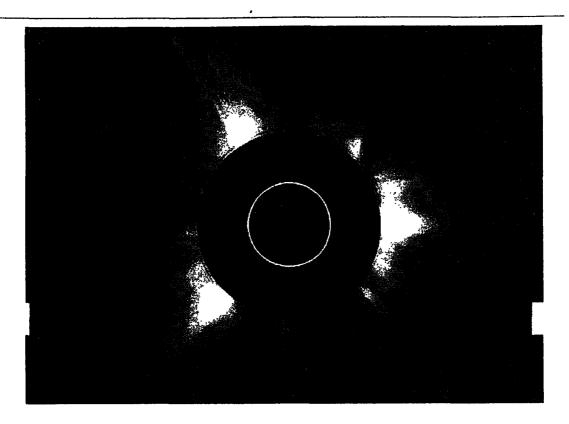
R. P. Lepping

NASA/Goddard

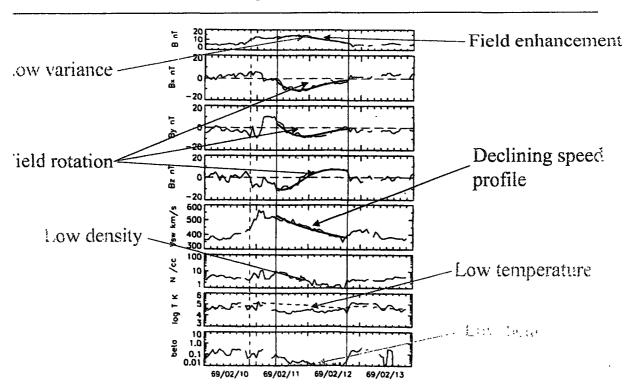
Overview

- Introduction
 - Coronal observations of CMEs
 - In situ observations of magnetic clouds
 - Modeling Flux ropes
- MHD modelling of CMEs
 - Coronal model (SAIC)
 - Heliospheric model (NOAA/SEC)
- Comparison with observations
 - ACE/Ulysses spring 1999 event
- Summary
- Future work

Introduction: White Light Observations of CMEs



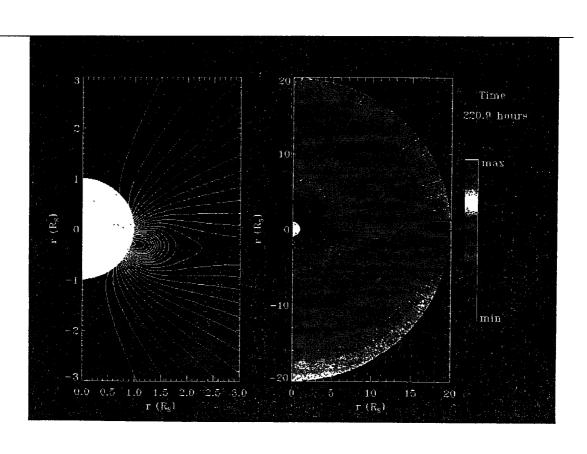
Introduction: In situ observations of magnetic clouds



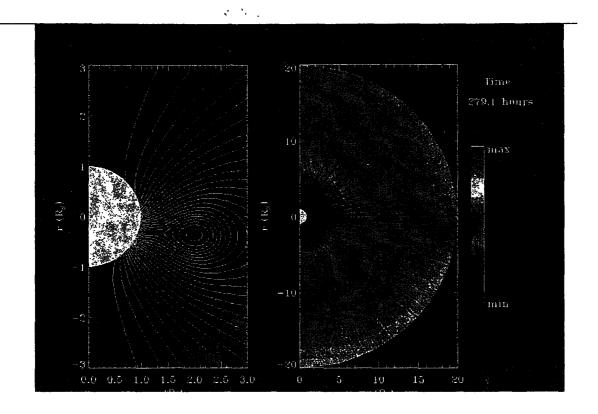
Introduction: Models of Magnetic clouds/flux ropes

- Kinematic Models:
 - Force-free
 - Force-free with expansion
 - None force-free with expansion
- Dynamic Models:
 - Fluid
 - **MHD**

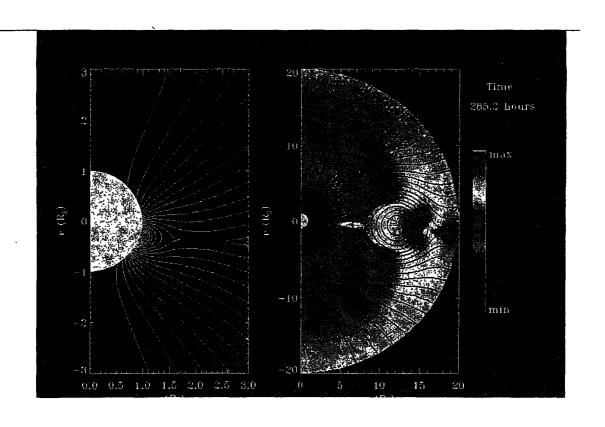
MHD Simulation: Coronal solution



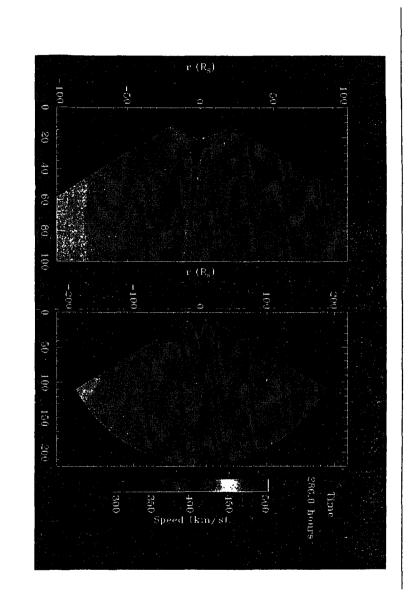
MHD Simulation: Coronal solution



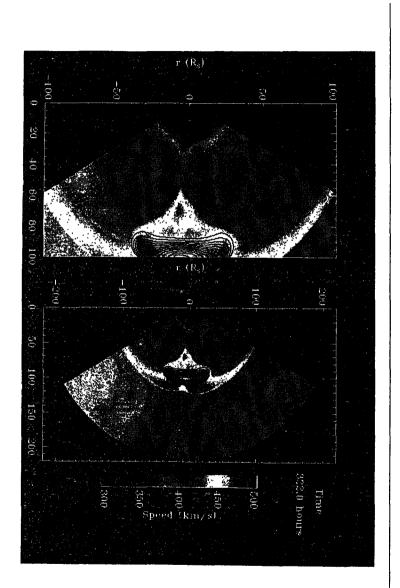
MHD Simulation: Coronal solution



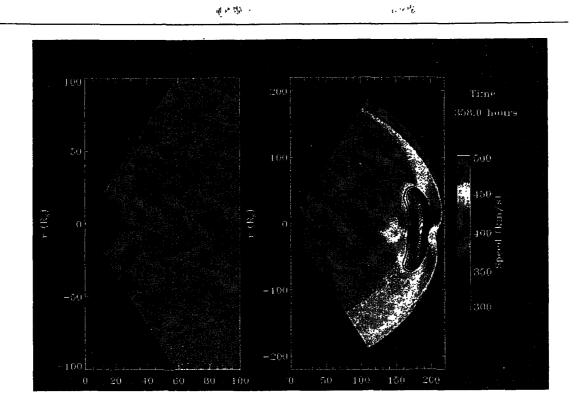
MHD Simulation: Heliospheric solution



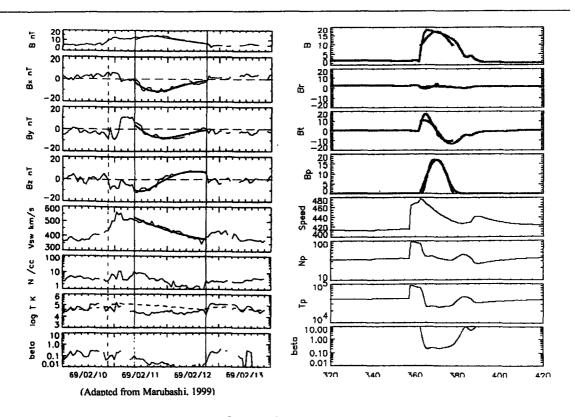
MHD Simulation: Heliospheric solution



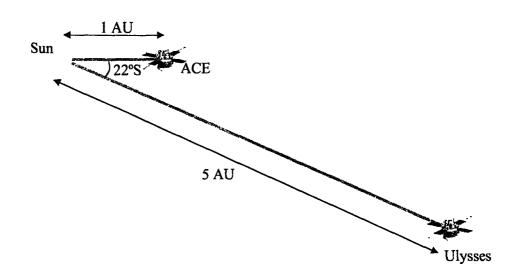
MHD Simulation: Heliospheric solution



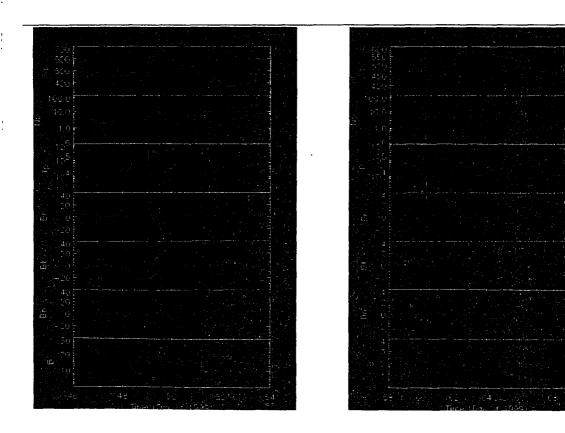
Comparison of an observed magnetic cloud with the generic simulation



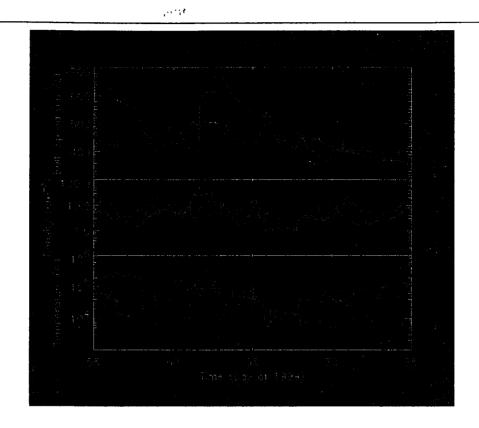
ACE/Ulysses Feb 1999 CME Event



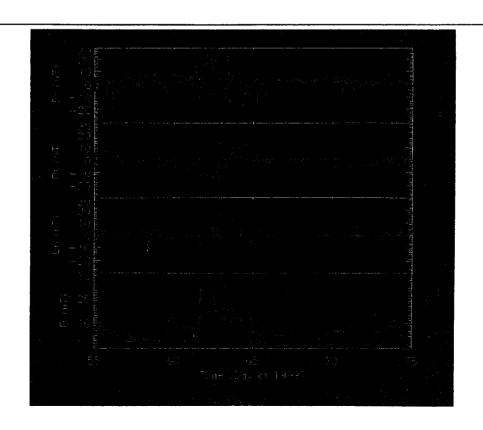
ACE/Ulysses Feb 1999 CME Event



Ulysses/ACE May 1999 CME



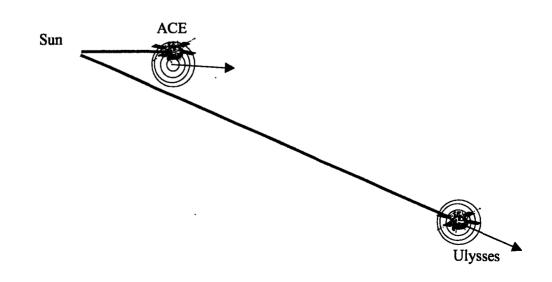
Ulysses/ACE May 1999 CME



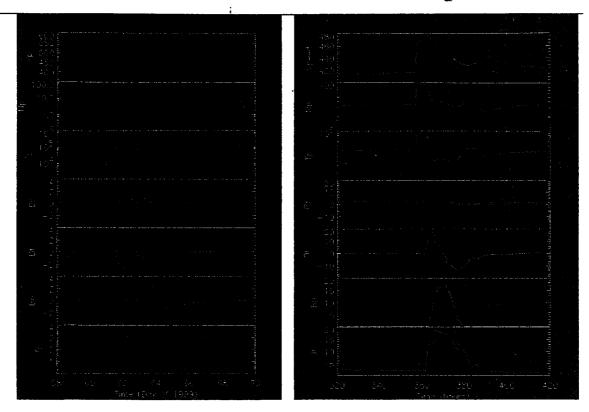
Force-Free Fitting at ACE and Ulysses

Parameter	ACE	Ulysses
Start (day hr:min)	49 14:00	62 20:00
Stop (day hr:min)	50 11:00	64 22:00
φ (deg)	282.1	271.1
θ (deg)	-1.3	53
y/R	0.738	0.0064
Helicity	-1	-1
R(AU)	0.28	0.34

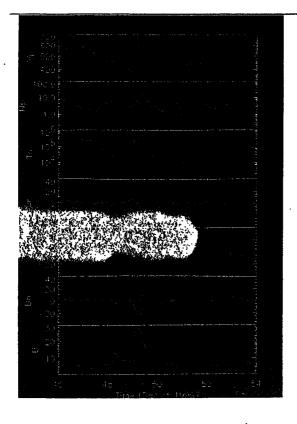
ACE/Ulysses Feb 1999 CME Event: Global structure from force-free fitting

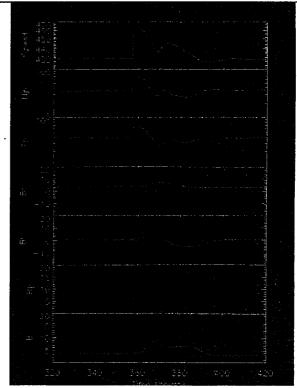


Comparison of in situ observations with MHD simulation: Ulysses



Comparison of in situ observations with MHD simulation: ACE





Deceleration of CME

Estimate time for CME to travel from ACE to Ulysses

$$V_{\text{CME}}(\text{ACE}) = 590 \text{ km/s}$$

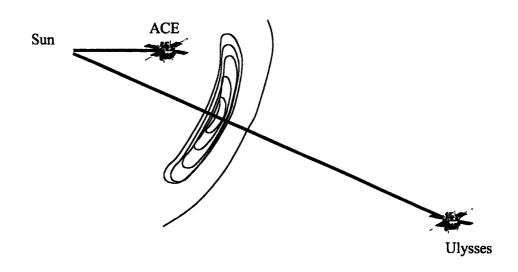
$$V_{\rm CME}({\rm Ulysses}) = 460 \, {\rm km/s}$$

Assume constant deceleration between 1 and 5 AU

$$=> \Delta t = 13.62 \text{ days}$$

- CME actually arrived 13.9 days later
- => Large-scale structure not significantly distorted

ACE/Ulysses Feb 1999 CME Event: Global structure



Summary

- Idealized MHD simulations:
 - provide global context for interpreting in situ CME observations
 - Emphasize significant role of dynamics on the evolution of ejecta and their associated disturbances
 - Identify new effects that can be searched for in observations

Future Studies

- Explore effects of different launch profiles
 - Do different mechanisms of eruptions lead to different interplanetary signatures?
- Launch CME in three dimensions
 - 3-D flow
 - Magnetic connectivity to Sun
- Incorporate composition into model

APPENDIX E

"Modeling of Transequatorial Loops with MH4D"

R. Lionello and D. Schnack

Presented at the Spring AGU Meeting

Boston, MA, May 29–June 2, 2001

Modeling of Transequatorial Loops with MH4D

R. Lionello

and

D. D. Schnack



Center for Energy and Space Science San Diego, CA



GOALS AND CHALLENGES

- Develop an efficient 3-D discrete representation for the resistive MHD model using an unstructured grid of tetrahedral cells
 - Truly arbitrary geometry
 - Use Cartesian coordinates
 - · Avoids coordinate singularities and complicated metrics
 - Apply to a variety of problems
 - Fusion
 - · Solar and space physics
 - ??

Challenges

- Discrete representation of differential operators
 - Compactness (couple only nearest neighbor grid points)
 - Self-adjointness
 - Annihilation properties (eg., $\nabla B = 0$)
- · Solution of implicit system
- · Grid generation
- Implementation
 - Code and data structure (OO techniques)
 - Parallelism
 - · Grid decomposition

THE FIRST CHALLENGE

Find efficiently computable discrete representations of the magnetic field and differential operators on a 3-D unstructured grid of tetrahedra

• The magnetic field and current density:

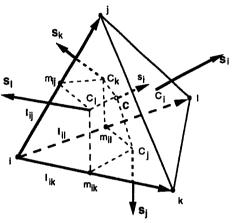
$$\mathbf{B} = \nabla \times \mathbf{A}, \qquad \mathbf{J} = \nabla \times \mathbf{B},$$

$$\mathbf{J} = \nabla \times \nabla \times \mathbf{A}$$

and consequently

- Both B and J are solenoidal
- The operator is self-adjoint: provided A, and A₂ satisfy the same boundary $\int \mathbf{A}_2 \cdot \nabla \times \nabla \times \mathbf{A}_1 dV = \int \mathbf{A}_1 \cdot \nabla \times \nabla \times \mathbf{A}_2 dV$ conditions
- Seek a discrete representation that retains these properties

GEOMETRY



- Sides are labeled by the index of their opposite vertex.
- C is the centroid of the tetrahedron.
- mij is the midpoint of edge lij.
- Ci is the centroid of side i.
- S_i is the vector area of side i.
- m_{ii} C_i , C, and C_k are coplanar.
- $\mathbf{s}_{\mathbf{i}}$ is the area of the dual median surface.

$$s_i = S_i/3$$

FINITE VOLUME METHOD

- Use integral relations to define differential operators
- Examples:

Gradient:

$$\int \nabla f dV = \int_{S} \hat{\mathbf{n}} f dS$$

Divergence:

$$\int \nabla \cdot \mathbf{F} dV = \int_{S} \hat{\mathbf{n}} \cdot \mathbf{F} dS$$

Curl (2-D):

$$\int_{S} \hat{\mathbf{n}} \cdot \nabla \times \mathbf{F} dS = \oint_{C} \mathbf{F} \cdot d\mathbf{I}$$

Curl (3-D):

$$\int \nabla \times \mathbf{F} dV = \int_{S} \mathbf{\hat{n}} \times \mathbf{F} dS$$

• Integrate over control volume (computational cell), eg.,

$$(\nabla f)_c = \frac{1}{V_c} \sum_{s} \hat{\mathbf{n}}_s f_s S_s$$

 We will apply this technique to tetrahedral and dual median volume elements

THE MAGNETIC FIELD

 The vector potential A is defined at vertices of tetrahedra

A varies linearly within a tetrahedron

• Integral definition:

$$\int \mathbf{B} dV = \int \nabla \times \mathbf{A} dV = \int_{S} d\mathbf{S} \times \mathbf{A}$$

• Apply to tetrahedral cell:

$$\mathbf{B}_{\tau}V_{\tau} = \sum_{s=1}^{4} \mathbf{S}_{s} \times \overline{\mathbf{A}}_{s}$$

 ${f B}_{ au}$ is constant within tetrahedron au ${f \overline{A}}_s$ is the average of ${f A}$ over the 3 vertices of side ${f S}$ ${f V}_{ au}$ is the volume of tetrahderon au

• In terms of vertices

$$\mathbf{B}_{\tau} = -\frac{1}{3V_{\tau}} \sum_{\nu(\tau)} \mathbf{S}_{\nu} \times \mathbf{A}_{\nu}$$

v(au) are the indices of the 4 vertices of tetrahedron au

 \mathbf{S}_{v} is the (outward directed) side opposite vertex v

DIVERGENCE OF B

• Apply Gauss' theorem to dual median volume element surrounding vertex ν

$$v_v = \sum_{\tau(v)} \frac{1}{3} V_{\tau}$$
 is the volume of this cell

$$\begin{split} \tau(v) & \text{ are the indices of the tetrahedra sharing vertex } v \\ & (\nabla \cdot \mathbf{B})_{v} v_{v} = \frac{1}{3} \sum_{\tau} \mathbf{B}_{\tau} \cdot \mathbf{S}_{v(\tau)} \\ & = \frac{1}{3} \sum_{\tau} \frac{1}{V_{\tau}} \sum_{\gamma(\tau)} \overline{\mathbf{A}}_{\gamma} \cdot \left(\mathbf{S}_{v} \times \mathbf{S}_{\gamma} \right) \end{split}$$

 $v(\tau)$ is the index of the side of tetrahedron τ opposite vertex v $\gamma(\tau)$ are the indices of the 4 sides of tetrahedron τ

- This gives:
- NOW A MIRACLE OCCURS!!!

 After some algebra, we find that the contributions from common faces of adjoining tetrahedra cancel exactly!
- The result!

$$(\nabla \cdot \mathbf{B})_{\nu} = 0$$

· Caveat: This holds for interior vertices only

ALTERNATE DERIVATION OF B

- A(x) varies linearly within a tetrahedron:
- Take the curl of this function in tetrahedron τ .

$$\mathbf{A}(\mathbf{x}) = \sum_{\nu} \mathbf{A}_{\nu} \left[1 - \frac{1}{3V_{\tau}} \mathbf{S}_{\nu} \cdot (\mathbf{x} - \mathbf{x}_{\nu}) \right]$$

• The result is:

$$\mathbf{B}_{\tau} = \frac{B_{\alpha}}{3V_{\tau}} \underbrace{\frac{\partial A_{\gamma}}{\partial \mathbf{v}_{\tau}}}_{\mathbf{v}(\tau)} \underbrace{\frac{\partial A_{\gamma}}{\partial \mathbf{v}_{\beta}}}_{\mathbf{A}_{\nu}} \mathbf{A}_{\nu}$$

- Identical to the finite-volume expression!
- Demonstrates first order accuracy (exact for linear functions)
- Have been unable to show second order accuracy

THE CURRENT DENSITY

• Use generalized Stokes' formula as applied to dual median volume element

$$\int \mathbf{J}dV = \int \nabla \times \mathbf{B}dV = \int_{S} \hat{\mathbf{n}} \times \mathbf{B}dS$$
$$\mathbf{J}_{v}v_{v} = \frac{1}{3} \sum_{\tau(v)} \mathbf{S}_{v(\tau)} \times \mathbf{B}_{\tau}$$

$$\mathbf{J}_{\nu}V_{\nu} = \sum_{\tau(\nu)\nu'(\tau)} \mathbf{M}^{\tau}(\nu,\nu') \cdot \mathbf{A}_{\nu'}$$
$$\mathbf{M}^{\tau}(\nu,\nu') = \frac{1}{9V_{\tau}} \left[\left(\mathbf{S}_{\nu(\tau)} \cdot \mathbf{S}_{\nu'(\tau)} \right) \mathbf{I} - \mathbf{S}_{\nu'(\tau)} \mathbf{S}_{\nu(\tau)} \right]$$

- Substituting the expression for B in terms of A:
- Symmetry:

$$M_{\alpha\beta}^{\tau}(v,v')=M_{\beta\alpha}^{\tau}(v',v), \quad \alpha,\beta=x,y,z$$

• This is the discrete "curl-curl" operator

SELF-ADJOINTNESS

• Define inner product:

$$(\mathbf{P}, \mathbf{Q}) = \int \mathbf{P} \cdot \mathbf{Q} dV = \sum_{\tau=1}^{N_{\tau}} \sum_{\nu(\tau)} \frac{1}{4} V_{\tau} \mathbf{P}_{\nu} \cdot \mathbf{Q}_{\nu}$$

• L is self-adjoint if:

$$(\mathsf{P}, L \cdot \mathsf{Q}) = (\mathsf{Q}, L \cdot \mathsf{P})$$

• Direct calculation using symmetry of M:

$$(\mathbf{P}, \mathbf{M} \cdot \mathbf{Q}) = \sum_{\tau} \frac{1}{4} V_{\tau} \sum_{\nu} \sum_{\nu'} \mathbf{P}_{\nu} \cdot \mathbf{M}^{\tau} (\nu, \nu') \cdot \mathbf{Q}_{\nu'}$$

$$= \sum_{\tau} \frac{1}{4} V_{\tau} \sum_{\nu} \sum_{\nu'} \mathbf{Q}_{\nu'} \cdot \mathbf{M}^{\tau} (\nu', \nu) \cdot \mathbf{P}_{\nu}$$

$$= \sum_{\tau} \frac{1}{4} V_{\tau} \sum_{\nu} \sum_{\nu'} \mathbf{Q}_{\nu} \cdot \mathbf{M}^{\tau} (\nu, \nu') \cdot \mathbf{P}_{\nu'}$$

$$= (\mathbf{Q}, \mathbf{M} \cdot \mathbf{P})$$

• The discrete operator is self-adjoint

VARIATIONAL PRINCIPLE

Minimize functional

$$I(\mathbf{A}) = \frac{1}{2} \int \left[(\nabla \times \mathbf{A})^2 - 2\mathbf{J} \cdot \mathbf{A} \right] dV$$

Variation of A: let

$$A \rightarrow A + \varepsilon \delta A$$

$$I(\mathbf{A} + \varepsilon \delta \mathbf{A}) = \frac{1}{2} \int \left[(\nabla \times \mathbf{A})^2 - 2 \mathbf{J} \cdot \mathbf{A} \right] dV$$
$$+ \varepsilon \int (\nabla \times \mathbf{A} \cdot \nabla \times \delta \mathbf{A} - \mathbf{J} \cdot \delta \mathbf{A}) dV$$
$$+ \frac{1}{2} \varepsilon^2 \int (\nabla \times \delta \mathbf{A})^2 dV$$

• For minimum, coefficient of ε must vanish:

$$\int \delta \mathbf{A} \cdot (\nabla \times \nabla \times \mathbf{A} - \mathbf{J}) dV = -\int_{S} \delta \mathbf{A}_{t} \cdot (\mathbf{B} \times \hat{\mathbf{n}}) dS$$
$$\mathbf{A}_{t} = (\mathbf{I} - \hat{\mathbf{n}} \hat{\mathbf{n}}) \cdot \mathbf{A}$$

• Natural boundary condition:

 $\delta \mathbf{A}_t = 0$, or \mathbf{A}_t specified on boundary (Dirichlet)

• Solutions $\nabla \times \nabla \times A = J$, with J specified in V, and A_i , specified on the boundaries, minimize I(A).

DISCRETE MINIMIZATION

- Minimize /(A) on a grid with N_ν vertices and N_τ tetrahedra
- Expand A(x) in basis functions

$$\mathbf{A}(\mathbf{x}) = \sum_{\nu} \mathbf{A}_{\nu} \alpha_{\nu}(\mathbf{x})$$

• Expand J in delta-functions

$$\mathbf{J}(\mathbf{x}) = \sum_{\nu} \mathbf{v}_{\nu} \mathbf{J}_{\nu} \delta(\mathbf{x} - \mathbf{x}_{\nu})$$

• Substitute into /(A):

$$I = \frac{1}{2} \sum_{v} \sum_{v'} \left[\mathbf{A}_{v} \cdot \mathbf{M} \left(v, v' \right) \cdot \mathbf{A}_{v'} - v_{v} \mathbf{J}_{v} \cdot \mathbf{A}_{v'} \alpha_{v'} (\mathbf{x}_{v}) \right]$$

$$\mathbf{M} \left(v, v' \right) = \left[\left[\left(\nabla \alpha_{v} \cdot \nabla \alpha_{v'} \right) \mathbf{I} - \nabla \alpha_{v'} \nabla \alpha_{v} \right] dV$$

• To minimize, set

$$\frac{\partial I}{\partial A_{\gamma,\nu}}=0, \qquad \gamma=x,y,z$$

• Result:

$$\left(\sum_{\nu} \alpha_{\mu}(\mathbf{x}_{\nu})\right) v_{\nu} \mathbf{J}_{\nu} = \sum_{\tau} \sum_{\nu} \mathbf{M}^{\tau}(\mu, \nu) \cdot \mathbf{A}_{\nu}, \quad \mathbf{M} = \sum_{\tau} \mathbf{M}^{\tau}$$

• With tent expansion functions ($\alpha_{\mu}(\mathbf{x}_{\nu})=\delta_{\mu\nu}$), gives finite volume expression

BOUNDARY CONDITIONS

- No reference to boundary conditions in discrete minimization
- Discrete expression for the "curl-curl" operator is 3N, equations in 3N, unknowns
 Could be solved for all unknowns, including all values at the M, boundary vertices
- Absence of surface term implies that solution will satisfy the natural boundary condition

$$\delta \mathbf{A}_t \cdot (\mathbf{B} \times \hat{\mathbf{n}}) = 0$$

- Since A, is *not* fixed, this can be satisfied only if $\mathbf{B} \times \hat{\mathbf{n}} = 0$
- Constraint on source and surface field: Solutions with vanishing tangential magnetic field $\int_{\mathcal{S}} dS \hat{\mathbf{n}} \times \mathbf{B} = \int \mathbf{J} dV$
 - exist only if total current vanishes
- In general, we must specify A, on the boundary

ALTERNATE BOUNDARY CONDITIONS

 Must include surface term in the functional to be minimized

$$I(\mathbf{A}) = \int \left[(\nabla \times \mathbf{A})^2 - 2\mathbf{J} \cdot \mathbf{A} \right] dV + \int_{S} (\mathbf{A}_t \cdot \mathbf{P} - 2\mathbf{Q}) \cdot \mathbf{A}_t dS$$

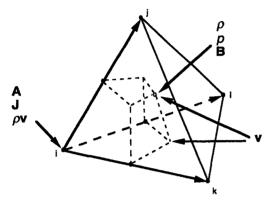
P is a self - adjoint matrix and Q is a vector

Performing variation and minimization as before leads to the condition

$$\int \delta \mathbf{A} \cdot (\nabla \times \nabla \times \mathbf{A} - \mathbf{J}) dV + \int \delta \mathbf{A}_t \cdot (\mathbf{B} \times \hat{\mathbf{n}} + \mathbf{P} \cdot \mathbf{A}_t - \mathbf{Q}) dS = 0$$

- Since the tangential variation no longer vanishes at the surface, this can be satisfied only if
- Mixed (von Neumann/Dirichlet) boundary
 ∇×∇×A = J in V, and B×n+P·A_t = Q on S
 condition
- Allows specification of tangential magnetic field
- Could apply discrete minimization to this modified functional to obtain more formalism that accommodates these boundary conditions

MHD FORMULATION



• Vertices:

A, **J**, and ρ **v**

• Centroids:

 ρ , p, and **B**

- Velocity averaged to faces or centroids, as required
- All quantities advanced in time by applying conservation laws to control volume
- Use the NIMROD anisotropic semi-implicit operator

SUMMARY AND STATUS

- Developed a formalism for defining A, B, and J on an unstructured grid of tetrahedra
- Finite-volume approach
- B is solenoidal
- "curl-curl" operator is compact and self-adjoint
- Solutions of discrete equations minimize the same functional as solutions of differential equations
- Tangential A can be specified on boundary
 - Can be generalized to specify tangential B
- Caveats:
 - Demonstrated only first order accuracy
 - . B is solenoidal only on interior vertices
 - · Have not demonstrated that J is solenoidal
- Solved model implicit resistive diffusion problem
- Starting point for full MHD model

PRELIMINARY VALIDATION

- Successive application of ∇× operators on primary and dual grids is identical to the composite ∇×∇× operator
- Verified that $\nabla \cdot \mathbf{B} = 0$
- Solution of diffusion equation in cubic, cylindrical, and spherical domains
 - Comparison with analytic solutions
- Single and multiple processor calculations yield identical results
- Future directions
 - More complex geometry
 - Magnetostatic problem
 - · Must deal with gauge condition
 - · Reconstruction of force-free fields from boundary data
 - Resistive MHD

Implementation

- Standard Fortran 90
 - Object-oriented features

http://www.cs.rpi.edu/~szymansk/oof90.html

- Parallelization
 - Runs on serial and parallel machines
 - MPI

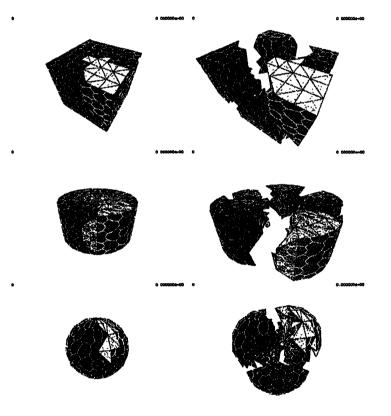
http://www.mpi-forum.org

Grid generation with LaGriT (LANL)
 http://www.t12.lanl.gov/~lagrit

Implementation (cont.)

- Grid decomposition with Metis (U.Minn.) http://www.cs.unm.edu/~metis
- Matrix inversion with PETSc (ANL) http://www.mcs.anl.gov/petsc
- Graphics with GMV (LANL)
 http://www-xdiv.lanl.gov/XCM/gmv/

Mesh Partitioning between 5 PEs



Test Case: Diffusion Equation

The diffusion equation for the vector potential **A**,

$$\frac{\partial \mathbf{A}}{\partial t} = -\eta \nabla \times \nabla \times \mathbf{A} + \mathbf{S},$$

is numerically implemented as

$$\Delta V \left(\frac{1}{\eta} + \omega \Delta t \nabla \times \nabla \times \right) \Delta \mathbf{A} = -\Delta V \Delta t \nabla \times \nabla \times \mathbf{A}^n + \frac{\Delta V \Delta t}{n} \mathbf{S}.$$

 ΔV Element of volume

 Δt Time step

 η Resistivity

 ω Factor between 1/2 and 1

S Source term

The operator on $\triangle A$ is self-adjoint in our formulation.

Numerical vs. Analytical Solution of Diffusion Equation: Box

• A solution of the diffusion equation in a box domain:

$$A_z = \exp(-
u t) \sin\left(rac{n_x \pi x}{L_x}
ight) \sin\left(rac{n_y \pi y}{L_y}
ight)$$

• If

$$L_x = L_y = n_x = n_y = 1,$$

 $\eta = 0.01$

Then

$$\nu_{\text{Analytical}} = 0.197.$$

• Using 125 nodes, 383 cells in a $1 \times 1 \times 1$ cubic domain and $\Delta t = 0.01$,

$$\nu_{\text{Numerical}} = 0.182.$$

Numerical vs. Analytical Solution

of Diffusion Equation: Sphere

 A solution of the diffusion equation in a sphere:

$$A_z = \exp(-\nu t) \left(\frac{\sin(kr)}{(kr)^2} - \frac{\cos(kr)}{(kr)} \right) \sin \theta$$

• If

$$k = 4.493$$

 $\eta = 0.01$

Then

$$\nu_{\rm Analytical} = 0.202$$

• Using 513 nodes, 2519 cells in a spherical domain of R=1 and $\Delta t=0.01$.

$$\nu_{\text{Numerical}} = 0.188$$

Numerical vs. Analytical Solution of Diffusion Equation: Cylinder

 A solution of the diffusion equation in a cylinder:

$$A_z = \exp(-\nu t) \mathsf{J}_0\left(kr\right)$$

• If

$$k = 2.405$$
 $n = 0.04$

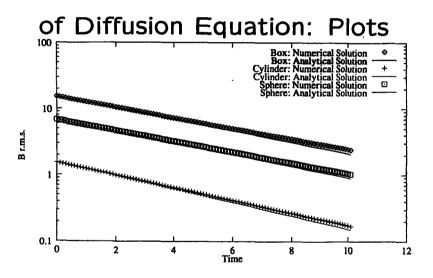
Then

$$\nu_{\mathsf{Analytical}} = 0.231$$

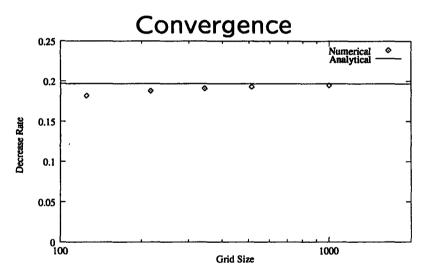
• Using 500 nodes, 1704 cells in a cylindrical domain of h=R=1 and $\Delta t=0.01$,

$$\nu_{\text{Numerical}} = 0.218$$

Numerical vs. Analytical Solution



Numerical vs. Analytical Solution of Diffusion Equation:



Density Advection

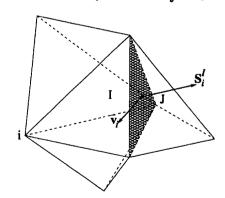
• Advection equation:

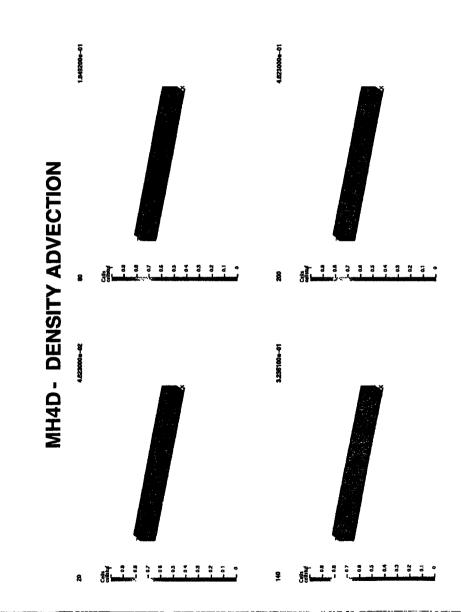
$$\frac{\partial \rho}{\partial t} = -\nabla \cdot \rho \mathbf{v}.$$

• Finite volume formulation with upwinding:

$$\frac{\Delta \rho^I}{\Delta t} = -\frac{1}{V^I} \sum_i \mathbf{S}_i^I \cdot \bar{\mathbf{v}}_i \rho^{U(i)},$$

$$\rho^{U(i)} = \begin{cases} \rho^I & \text{if } \mathbf{S}_i^I \cdot \bar{\mathbf{v}}_i \ge 0 \\ \rho^J & \text{if } \mathbf{S}_i^I \cdot \bar{\mathbf{v}}_i < 0 \end{cases}$$





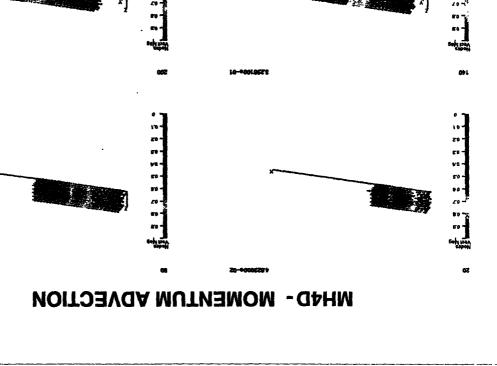
Momentum Advection

Advection equation:

$$\frac{\partial \mathbf{p}}{\partial t} = -\nabla \cdot \mathbf{p} \mathbf{v}.$$

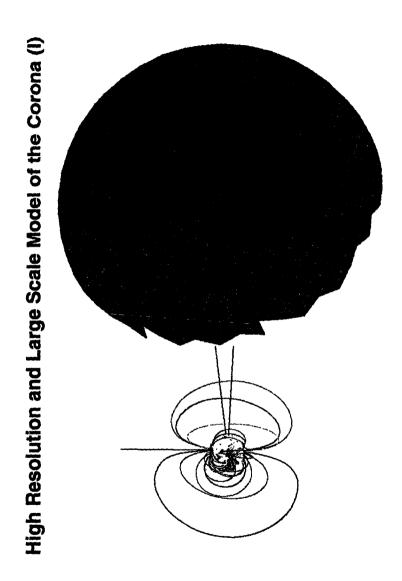
Finite volume formulation with upwinding:

$$rac{\Delta \mathbf{p}_i}{\Delta t} = -rac{1}{V_i} \sum_{\mathbf{E}} \mathbf{S}_i^{\mathbf{E}} \cdot ar{\mathbf{v}}^{\mathbf{E}} \mathbf{p}_u(\mathbf{E}),$$
 $\mathbf{p}_u(\mathbf{E}) = egin{cases} \mathbf{p}_i & \text{if } \mathbf{S}_i^{\mathbf{E}} \cdot ar{\mathbf{v}}^E \geq 0 \\ \mathbf{p}_j & \text{if } \mathbf{S}_i^{\mathbf{E}} \cdot ar{\mathbf{v}}^E < 0 \end{cases}$

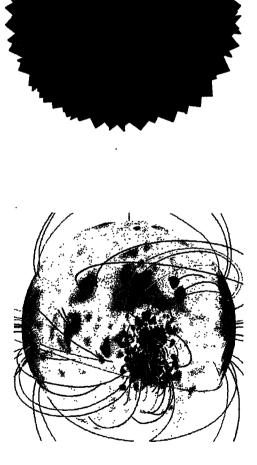


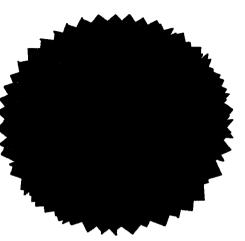
Potential Models

- Active region during Whole Sun Month (August-September 1996).
- Active regions AR8102 and AR8100 (November 1997).
- We use synoptic magnetograms from Kitt Peak National Observatory.
- The grid extends from 1 to 10 R_{\odot} .
- The meshes consist of 42001 (32881) vertices and 242705 (189237) tetrahedra.
- The resolution varies from 8 degrees (outside the active regions) to 1 degree (inside).

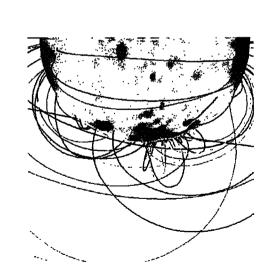


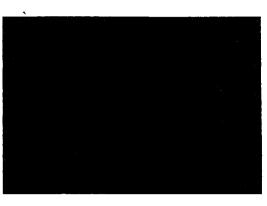
High Resolution and Large Scale Model of the Corona (II)



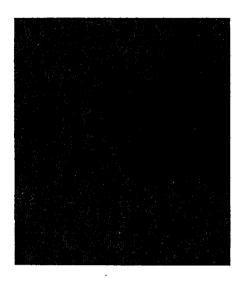


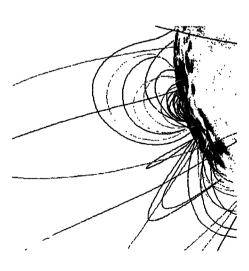
High Resolution and Large Scale Model of the Corona (III)



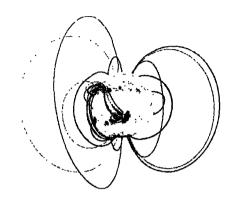


High Resolution and Large Scale Model of the Corona (IV)

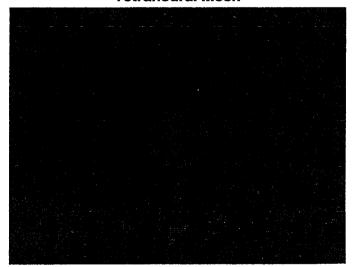




Magnetogram Data and Field Lines



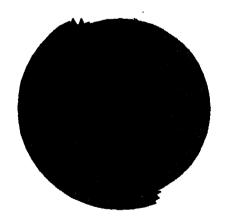
Tetrahedral Mesh



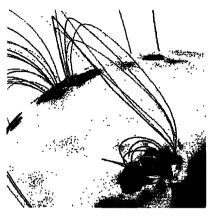
Magnetogram Data and Field Lines



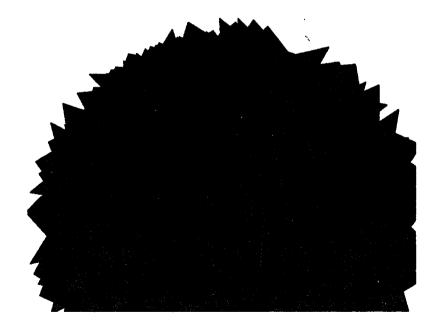
Tetrahedral Mesh



Magnetogram Data and Field Lines



Tetrahedral Mesh



REPORT DOCUMENTATION PAGE

Form Approved OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Artington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20506.

1. AGENCY USE ONLY (Leave Blank		3. REPORT TYPE	REPORT TYPE AND DATES COVERED 2nd Year 4th Quarter Progress Report	
			5. FUNDING NUMBERS NAS5-99188	
6. AUTHORS Zoran Mikic				
Science Applications International Corporation SAIC-C			8. PERFORMAING ORGANIZATION REPORT NUMBER SAIC-01/8013:APPAT-280 01-0157-04-2065-000	
			10. SPONSORING/MONITORING AGENCY	
NASA Headquarters Operation Office Goddard Space Flight Center Greenbelt, MD 20771			REPORT NUMBER	
11. SUPPLEMENTARY NOTES		1		
12a. DISTRIBUTION/AVAILABILITY S	STATEMENT		12b. DISTRIBUTION CODE	
13. ABSTRACT (Maximum 200 words	5)			
This report details progress during the fourth quarter of the second year of the Sun-Earth Connections Theory Program contract, "The Structure and Dynamics of the Solar Corona and Inner Heliosphere."				
14. SUBJECT TERMS			15. NUMBER OF PAGES .	
Solar Corona, Coronal Magnetic Field, Heliosphere, Magnetohydrodynamics			64	
			16. PRICE CODE	
17. SECURITY CLASSIFICATION OF REPORT	18. SECURITY CLASSIFICATION OF THIS PAGE	19. SECURITY CLASSIFICA OF ABSTRACT	ATION 20. LIMITATION OF ABSTRACT	
UNCLASSIFIED	UNCLASSIFIED	UNCLASSIFIED	UL	